

# Noise-aware method for Speech Enhancement

汇报人：朱清扬

# CONTENTS

1

Introduction

2

Basic methods and theoretical basis

3

Experiment results



# PART 01

## Introduction



# Introduction

Weiner  
Filtering

- the signal keeps stable
- Statistical properties remains the same.



VAE-NMF

Train for VAE-NMF

- NMF can just produce limited noise
- Standard VAE is sensitive to noise



NAE



# PART 02

Basic methods  
and theoretical basis



# Basic methods

## Spectrum Subtraction

Spectral subtraction is based on a **simple assumption**: The noise in speech is only **additive noise**

$$\text{let } D(\omega) = P_S(\omega) - P_N(\omega)$$
$$P'_S(\omega) = \begin{cases} D(\omega), & \text{if } D(\omega) > 0 \\ 0, & \text{otherwise} \end{cases}$$

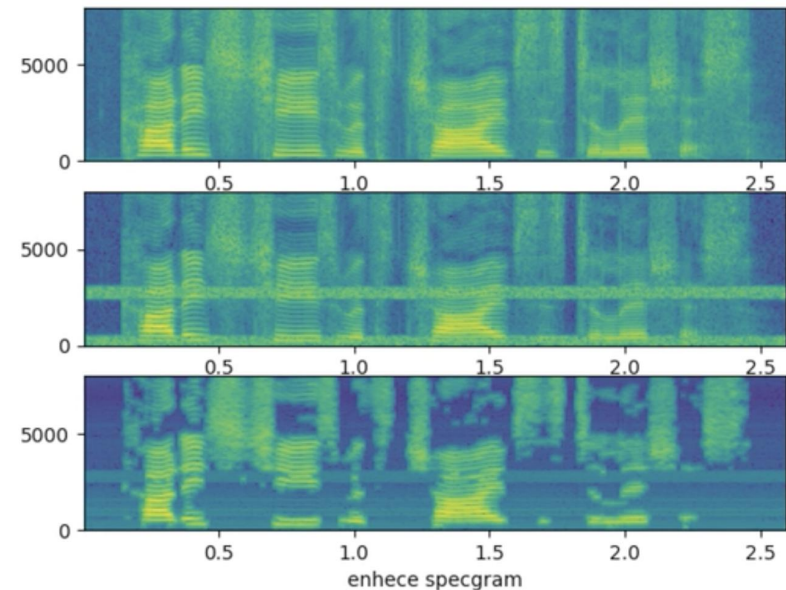
*'music noise!'*

$$\text{let } D(\omega) = P_S(\omega) - \alpha P_N(\omega)$$
$$P'_S(\omega) = \begin{cases} D(\omega), & \text{if } D(\omega) > \beta P_N(\omega) \\ \beta P_N(\omega), & \text{otherwise} \end{cases}$$

with  $\alpha \geq 1$ , and  $0 < \beta \ll 1$

$P_n$ : Generally, it is assumed that the first N frames of the input speech is the silence time, that is, there is no voice input during this time, only noise, which can be called **the floor noise**.

- $\alpha > 1$ : In this way, compared with the previous method, it can ensure a stronger denoising effect and can remove most of the noise, so that the residual noise will be much less.
- $0 < \beta \ll 1$ : The advantage of setting a lower limit is that the residual peak is less significant.



# Basic methods

## Wiener Filtering

- **simple assumption:** The observed signal  $X(k)$  and the random noise  $b(k)$  (independent of the source signal) are zero-mean and steady-state.

- **General function** for SISO model:  $x = s + n$ ;  $s = \text{speech}$ ,  $n = \text{noise}$ ,  $x = \text{noisy data}$

$$\hat{s} = h * x \quad ; \hat{s}: \text{est. speech.}$$

- **main object:**  $\min E(|\hat{s} - s|^2)$   
 $J = E(|s|^2) - hP_{xs} - \bar{h}P_{xs}^* + |h|^2P_{xx}$ ;  
 $P_{xs} = E(x\bar{s}); P_{xx} = E(|x|^2)$

- Take the derivative with respect to  $h$ :

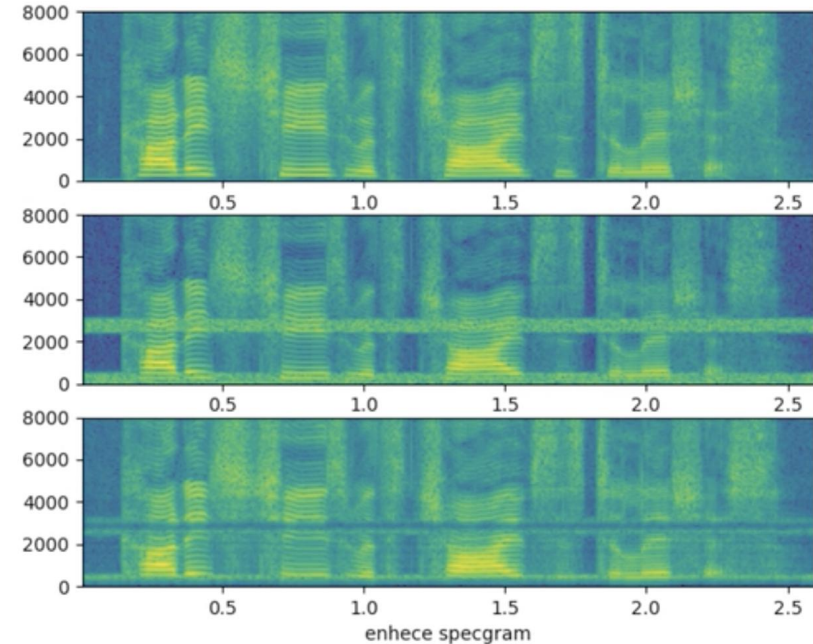
$$\frac{\partial J}{\partial h} = \bar{h}P_{xx} - P_{xs} = [hP_{xx} - P_{xs}]^* = 0$$

$$h = \frac{P_{xs}^*}{P_{xx}}$$

- In the case of speech enhancement :  
 $x = s + n$  ,  $s$  and  $n$  are independent with zero means.

$$P_{xs} = P_{ss}$$

$$P_{xx} = P_{nn} + P_{ss}$$



# VAE-NMF

## Definitions:

- STFT domain:  $(f, n) \in \{0, \dots, F - 1\} \times \{0, \dots, N - 1\}$   
noisy data  $X = (x_{f,n})$
- {speech data  $S = (s_{f,n})$   
noise data  $B = (b_{f,n})$
- Latent space:  $Z = (z_n), Z \in R^{L \times N}$

## Aim:

To find the most appropriate parameters to the model:

$$x_{f,n} = \sqrt{g_n} s_{f,n} + b_{f,n} .$$

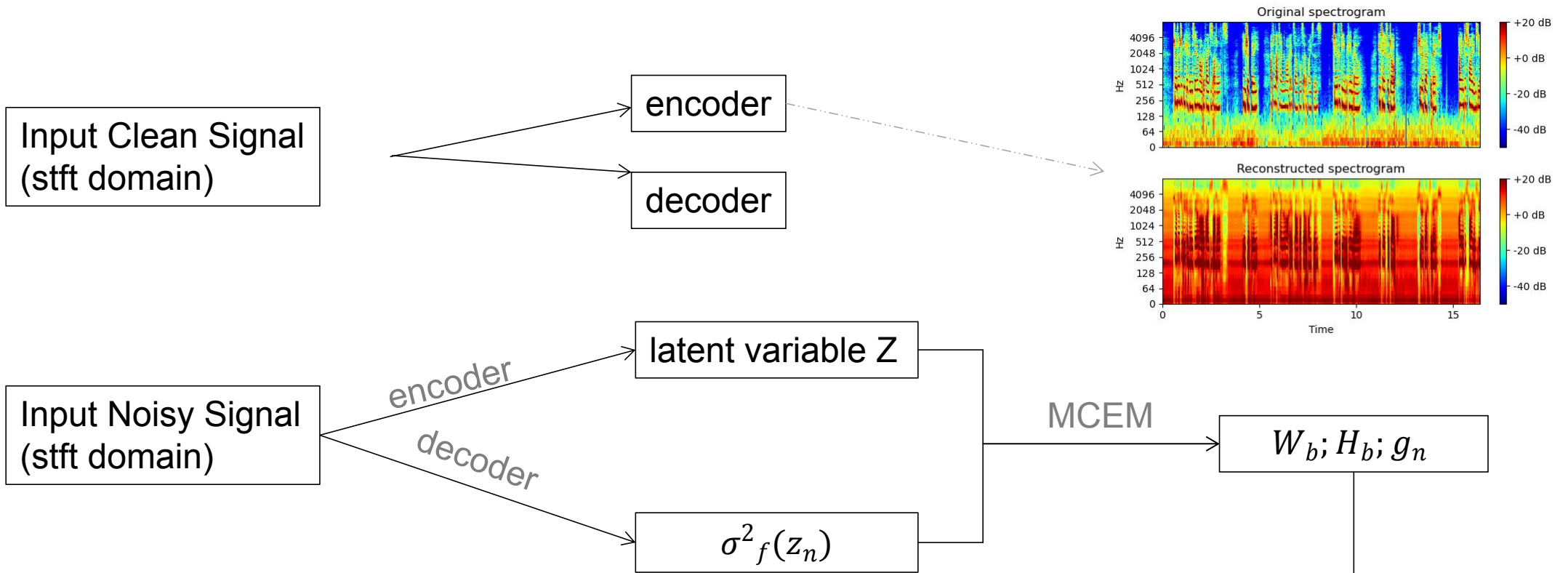
## Parameters:

- $s_{f,n} \sim N(0, \sigma^2_f(z_n))$  :  $\sigma^2_f(z_n)$  is defined by a Decoder;
- $b_{f,n} \sim N(0, (W_b H_b)_{f,n})$  :  $W_b H_b$  is a NMF of the noise vector;
- $\sqrt{g_n}$  : represents a frame-dependent but frequency-independent gain.



# VAE-NMF

baseline



speech reconstruction:

$$\begin{aligned}
 \hat{s}_{fn} &= \mathbb{E}_{p(\tilde{s}_{fn}|x_{fn};\theta_s,\theta_u^*)}[\tilde{s}_{fn}] \\
 &= \mathbb{E}_{p(\mathbf{z}_n|\mathbf{x}_n;\theta_s,\theta_u^*)} \left[ \mathbb{E}_{p(\tilde{s}_{fn}|\mathbf{z}_n,\mathbf{x}_n;\theta_s,\theta_u^*)}[\tilde{s}_{fn}] \right] \\
 &= \mathbb{E}_{p(\mathbf{z}_n|\mathbf{x}_n;\theta_s,\theta_u^*)} \left[ \frac{g_n^* \sigma_f^2(\mathbf{z}_n)}{g_n^* \sigma_f^2(\mathbf{z}_n) + (\mathbf{W}_b^* \mathbf{H}_b^*)_{f,n}} \right] x_{fn}.
 \end{aligned}$$

output speech data (clean data)

Weiner filter

# VAE-NMF

## MCEM

### EM method

- ▷ E-Step: Compute  $Q(\theta_u; \theta_u^*) = \mathbb{E}_{p(\mathbf{z}|\mathbf{x}; \theta_s, \theta_u^*)} [\ln p(\mathbf{x}, \mathbf{z}; \theta_s, \theta_u)]$ ;
- ▷ M-Step: Update  $\theta_u^* \leftarrow \arg \max_{\theta_u} Q(\theta_u; \theta_u^*)$ .

Problem:  $p(\mathbf{z}|\mathbf{x}, \theta_s, \theta_u)$  intractable!

### MH method:

- proposal distribution:  $\mathbf{z}_n | \mathbf{z}_n^{(m-1)}; \epsilon^2 \sim \mathcal{N}(\mathbf{z}_n^{(m-1)}, \epsilon^2 \mathbf{I})$ .
- acceptance:  $\alpha = \min \left( 1, \frac{p(\mathbf{x}_n | \mathbf{z}_n; \theta_s, \theta_u^*) p(\mathbf{z}_n)}{p(\mathbf{x}_n | \mathbf{z}_n^{(m-1)}; \theta_s, \theta_u^*) p(\mathbf{z}_n^{(m-1)})} \right)$ ,

### M-Step:

To maximize the Q function:

$$\mathbf{H}_b \leftarrow \mathbf{H}_b \odot \left[ \frac{\mathbf{W}_b^\top \left( |\mathbf{X}|^{\odot 2} \odot \sum_{r=1}^R (\mathbf{V}_x^{(r)})^{\odot -2} \right)}{\mathbf{W}_b^\top \sum_{r=1}^R (\mathbf{V}_x^{(r)})^{\odot -1}} \right]^{\odot 1/2}$$

$$\mathbf{W}_b \leftarrow \mathbf{W}_b \odot \left[ \frac{\left( |\mathbf{X}|^{\odot 2} \odot \sum_{r=1}^R (\mathbf{V}_x^{(r)})^{\odot -2} \right) \mathbf{H}_b^\top}{\sum_{r=1}^R (\mathbf{V}_x^{(r)})^{\odot -1} \mathbf{H}_b^\top} \right]^{\odot 1/2}$$

$$\mathbf{g}^\top \leftarrow \mathbf{g}^\top \odot \left[ \frac{\mathbf{1}^\top \left[ |\mathbf{X}|^{\odot 2} \odot \sum_{r=1}^R (\mathbf{V}_s^{(r)} \odot (\mathbf{V}_x^{(r)})^{\odot -2}) \right]}{\mathbf{1}^\top \left[ \sum_{r=1}^R (\mathbf{V}_s^{(r)} \odot (\mathbf{V}_x^{(r)})^{\odot -1}) \right]} \right]^{\odot 1/2}$$

### distributions in model:

- latent  $\mathbf{z}_n \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$ ;
- speech  $s_{fn} | \mathbf{z}_n; \theta_s \sim \mathcal{N}_c(0, \sigma_f^2(\mathbf{z}_n))$ ,
- noise  $b_{fn}; \mathbf{w}_{b,f}, \mathbf{h}_{b,n} \sim \mathcal{N}_c(0, (\mathbf{W}_b \mathbf{H}_b)_{f,n})$
- mixed voice  $x_{fn} | \mathbf{z}_n; \theta_s, \theta_{u,f,n} \sim \mathcal{N}_c(0, g_n \sigma_f^2(\mathbf{z}_n) + (\mathbf{W}_b \mathbf{H}_b)_{f,n})$

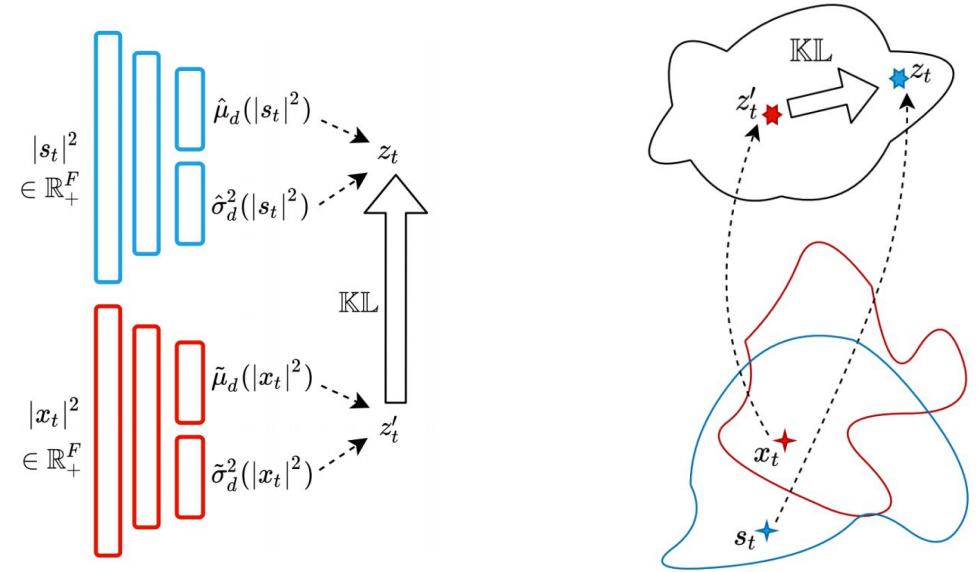
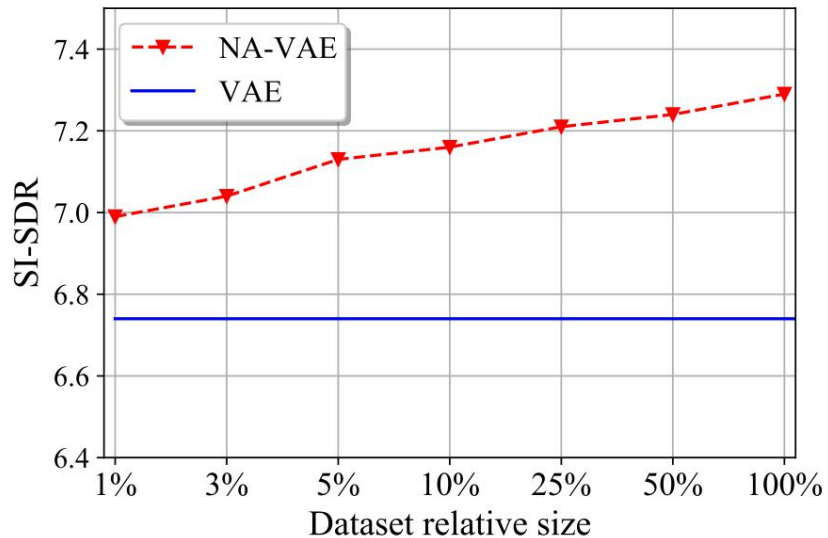
# NAE

Variational Autoencoder for Speech Enhancement with a Noise-Aware Encoder

## Two-step training (for encoder):

- Based on speech data, train an encoder, with the latent space  $Z$ .
- Based on noisy data, train the encoder to minimize:

$$\begin{aligned} \mathcal{L}(\gamma) &= \sum_t \text{KL}(q_\phi(z_t|s_t) || q'_\gamma(z'_t|x_t)) \\ &= \sum_{t,d} \left\{ \frac{1}{2} \log \frac{\tilde{\sigma}_d^2(|x_t|^2)}{\hat{\sigma}_d^2(|s_t|^2)} - \frac{1}{2} \right. \\ &\quad \left. + \frac{\hat{\sigma}_d^2(|s_t|^2) + (\hat{\mu}_d(|s_t|^2) - \tilde{\mu}_d(|x_t|^2))^2}{2\tilde{\sigma}_d^2(|x_t|^2)} \right\} \end{aligned}$$



- A technique to get the latent space: initialize the encoder with the trained data.
- Decoder got from traditional VAE, since the optimal mapping between latent space to clean data is difficult to get.



# PART 03

## Experiment results



# Results

Data when train and test:

- clean\_trainset\_wav\_16k: 11572pieces
- noisy\_trainset\_wav\_16k: 11572 pieces
- clean(noisy)\_testset\_wav\_16k: 2878pieces

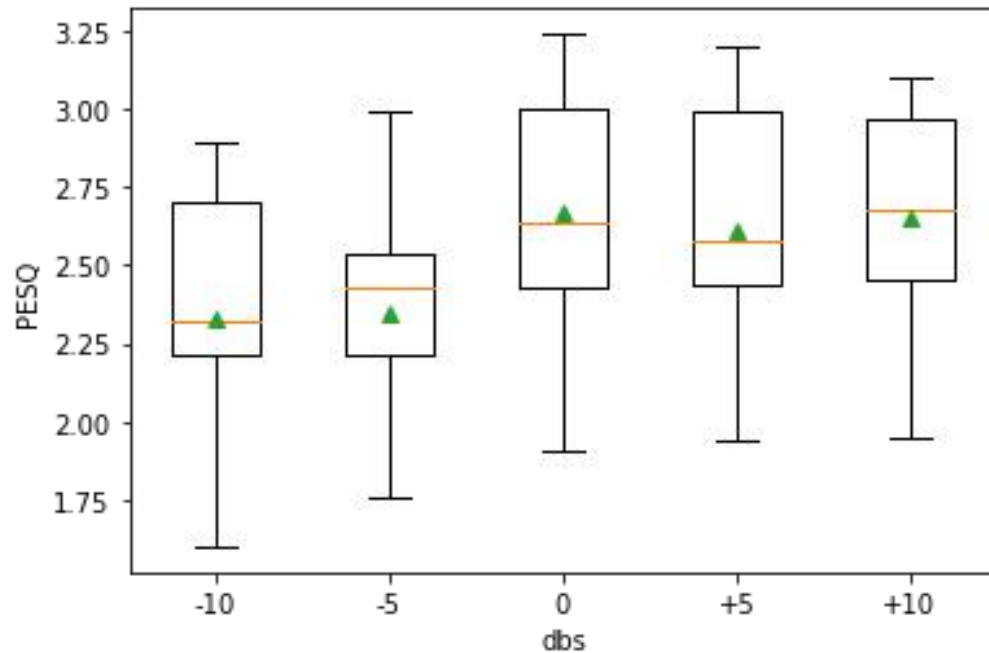


Figure 1. Performance comparison on PESQ with NAE on 5 different SNR cases.

SI-SDR	-10	-5	0	+5	+10
NAE	11.66	12.09	12.67	13.17	12.93
VAE-NMF	10.93	13.17	12.36	13.18	12.59
SS	7.89	10.81	10.90	11.19	11.01
WF	8.07	10.24	11.32	11.27	11.19
joint	10.90	12.13	12.19	12.38	12.56

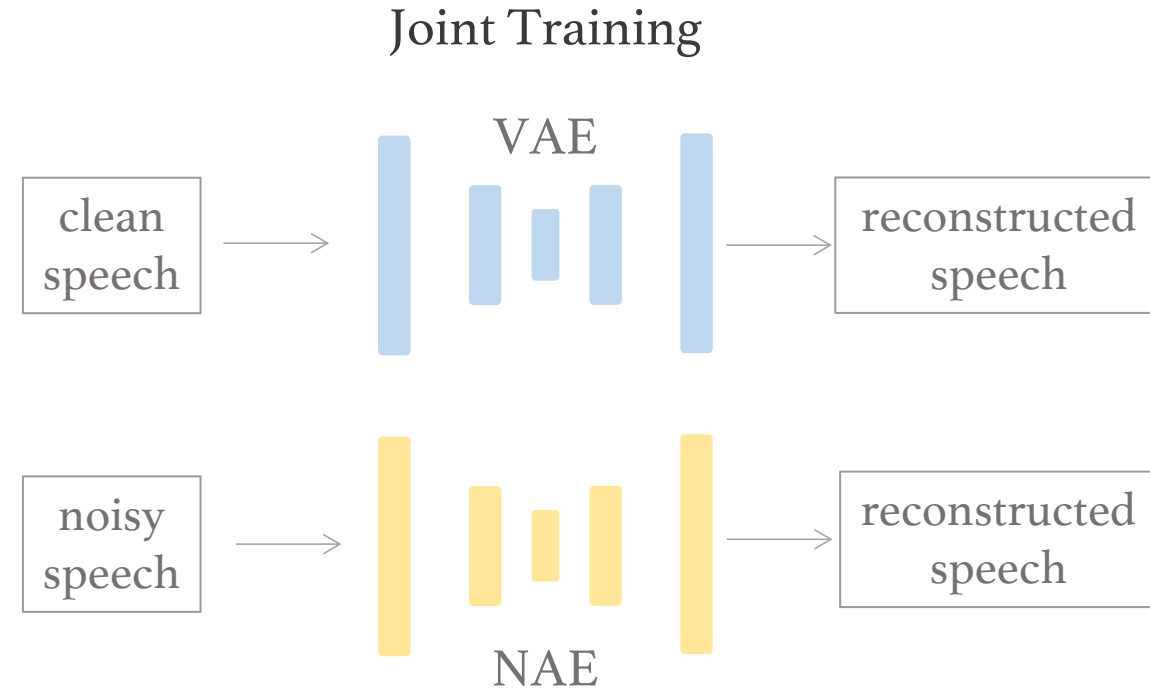
Figure 2. Performance comparison on SI-SDR on 5 different SNR cases and trained and evaluated on 5 similar methods.

# Results

Data:

- clean\_testset\_wav\_16k add white noise: 2878 pieces

SI-SDR	-10	-5	0	+5	+10
NAE	10.98	12.76	12.18	12.98	13.32
VAE-NMF	10.65	11.45	12.32	13.24	12.95
SS	6.77	8.29	8.78	8.91	10.03
WF	8.11	8.24	9.45	9.27	9.19
joint	10.18	11.25	11.98	12.87	13.01



$$loss = loss_{vae} + loss_{nae} + KL(z_{vae}|z_{nae})$$

Figure 3. Performance comparison on SI-SDR on 5 different SNR cases and trained and evaluated on 5 similar methods.



# THANKS FOR YOUR WATCHING

汇报人：朱清扬