

# Ontology Reasoning for the Semantic Web and Its Application to Knowledge Graph

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**Guilin Qi**

**Knowledge Science and Engineering (KSE) Lab**

**Southeast University**

**gqi@seu.edu.cn**



# Plan of the Talk

- ❑ **Part I: Introduction of Ontology Languages for the Semantic Web**
- ❑ **Part II: Application of Ontology Reasoning**
- ❑ **Part III: Reasoning with Large Imprecise Knowledge on the Semantic Web**

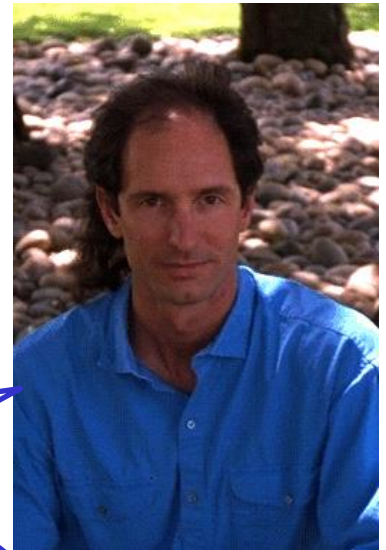


# Ontology

❑ Different definitions: philosophy, AI,...

❑ Definition in Semantic Web:

**An ontology is an explicit specification of a conceptualization**



Gruber, 1993

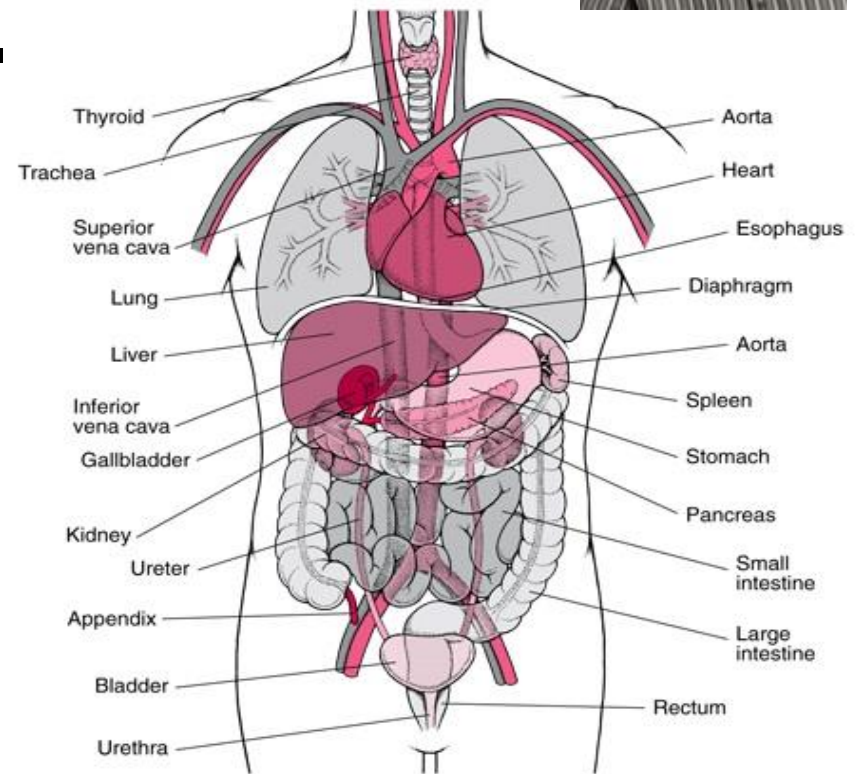


# What is an Ontology?

A model of (some aspect of) the world

□ Introduces vocabulary relevant to domain, e.g.

❖ **Anatomy**



# What is an Ontology?

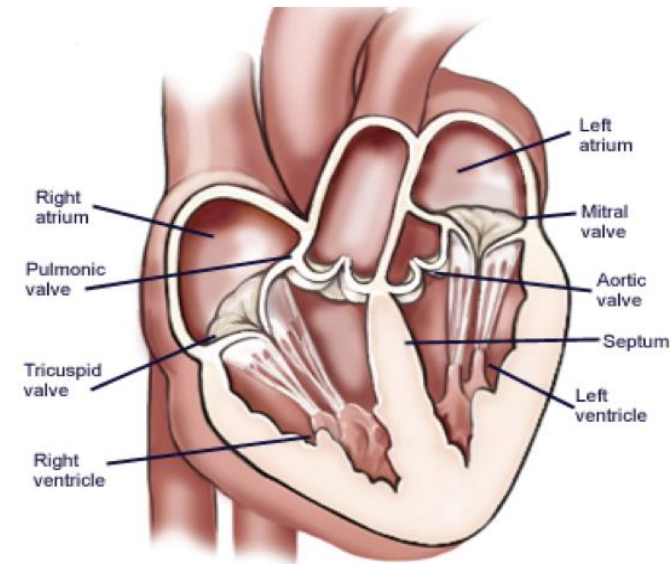


**A model of (some aspect of) the world**

□ **Introduces vocabulary relevant to domain**

□ **Specifies meaning (semantics) of terms**

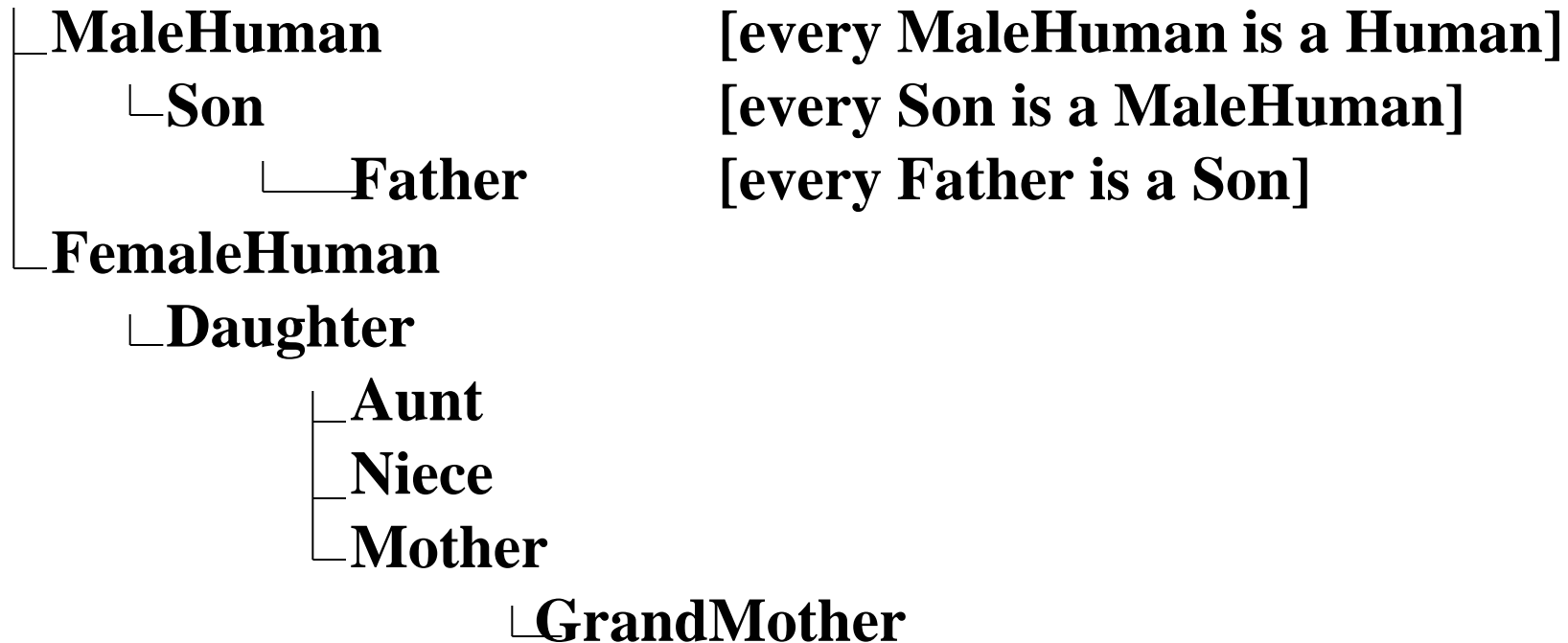
**Heart is a muscular organ that is part of the circulatory system**



# Ontologies

- The core of an ontology is usually a *taxonomy*:
  - ❖ classes of things, arranged in a hierarchy

## Human



# Ontology languages

- **RDF (Resource Description Framework)**
  - ❖ **Specifies relationship between data**
- **RDFS (Resource Description Framework Schema)**
  - ❖ **Specifies relationship between schema**
- **OWL (Web Ontology Language)**
  - ❖ **Specifies more complex relationship between schema based on description logics**



# RDF idea

- Use (directed) graphs as data model



- “Resource Description Framework”





# RDF Schema (RDFS)

- ❑ part of the W3C Recommendation RDF
- ❑ for schema/terminological knowledge
- ❑ uses RDF vocabulary with **pre-defined semantics**



# Classes and Instances

- ❑ **Classes stand for sets of things.  
In RDF: Sets of URIs.**
- ❑ **book:uri is a member of the class  
ex:Textbook**

```
book:uri    rdf:type    ex:Textbook .
```

- ❑ **a URI can belong to several classes**

```
book:uri    rdf:type    ex:Textbook .  
book:uri    rdf:type    ex:WorthReading .
```

- ❑ **classes can be arranged in hierarchies:  
each textbook is a book**

```
ex:Textbook  rdfs:subClassOf  ex:Book .
```



# Implicit knowledge

- if an RDFS document contains

```
u    rdf:type    ex:Textbook .
```

and

```
ex:Textbook    rdfs:subClassOf    ex:Book .
```

then

```
u    rdf:type    ex:Book .
```

**is *implicitly* also the case: it's a *logical consequence*. (We can also say it is *deduced* (deduction) or *inferred* (inference))**



# Implicit knowledge – another example

## □ From

```
ex:Textbook    rdfs:subClassOf    ex:Book .
```

```
ex:Book        rdfs:subClassOf    ex:PrintMedia .
```

**the following is a logical consequence:**

```
ex:Textbook    rdfs:subClassOf    ex:PrintMedia .
```

**I.e. `rdfs:subClassOf` is *transitive*.**



# Using implicit knowledge

Ontology (Knowledge Base)  
e.g. RDF or OWL



Reasoner (produces implicit knowledge)

offline



Completed (materialized) knowledge base

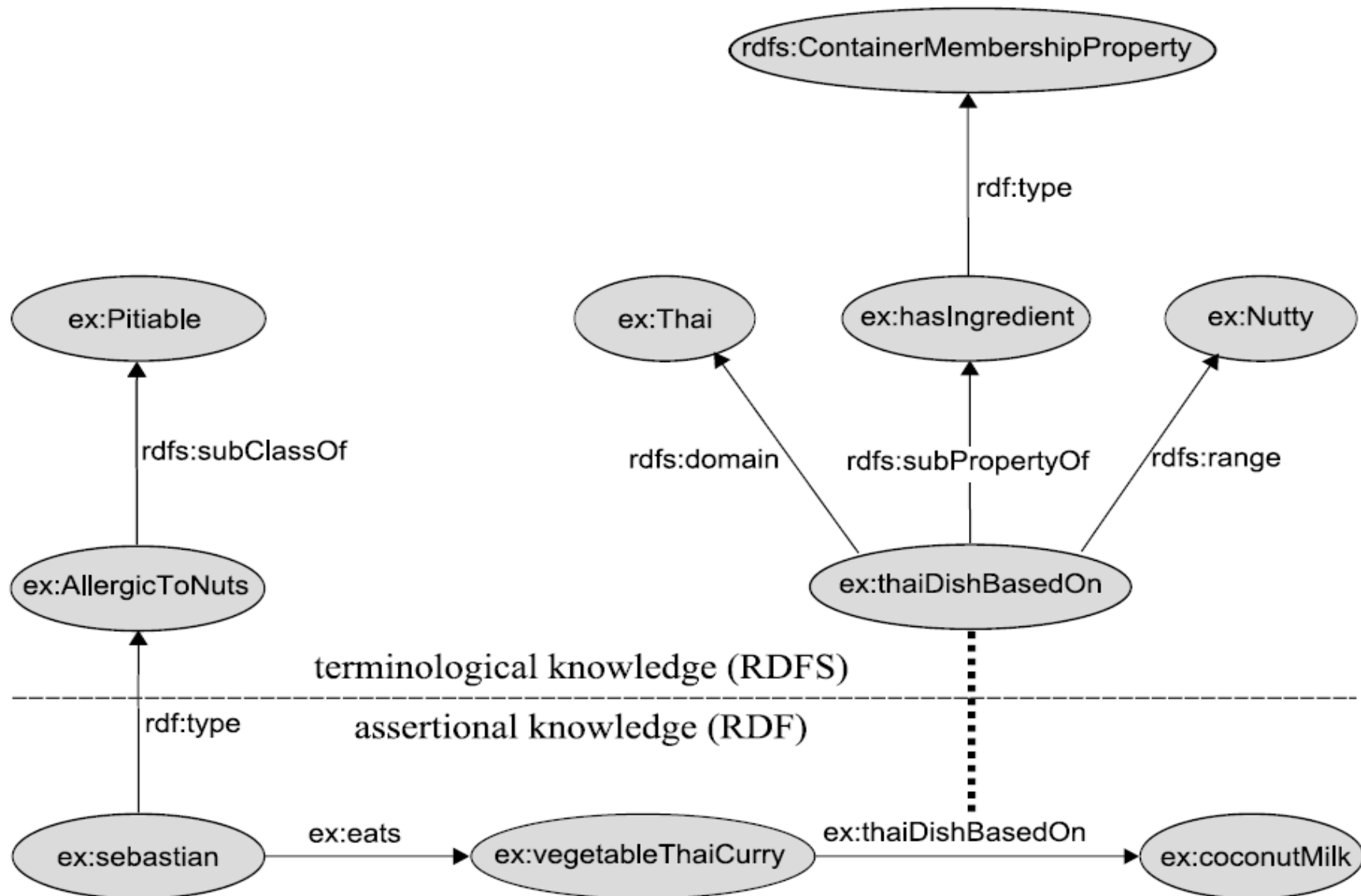
Used  
like a  
database



Application



# The same as graph



# OWL – Web Ontology Language

## Why do we need OWL?

**Project** Is either  
**Internal** or  
**External**

```
<owl:Class rdf:about="project">
  <rdfs:subClassOf>
    <owl:Class>
      <owl:unionOf
rdf:paseType="Collection">
        <owl:Class rdf:about="internal"/>
        <owl:Class rdf:about="external"/>
      </owl:unionOf>
    </owl:Class>
  </rdfs:subClassOf>
</owl:Class>
```



# OWL 2 Profiles

- The OWL 2 spec describes three profiles (fragments, sublanguages) which have polynomial complexity.
  - ❖ OWL EL (the description logic EL++)
    - Represent medical knowledge
  - ❖ OWL QL (the description logic DL Lite<sub>R</sub>)
    - Targeted to data integration
  - ❖ OWL RL (the description logic DLP)
    - inspired by intersecting OWL with Datalog
    - implemented e.g. in Oracle 11g





# Description Logics

## □ Description logics

- ❖ Are (mostly) decidable fragments of first-order predicate logic
- ❖ Provide logical underpinning of W3C standard OWL

## □ Building blocks

- ❖ Concepts (unary predicates/formulae with one free variable)
  - E.g., Person, Lawyer ⊆ Doctor
- ❖ Roles (binary predicates/formulae with two free variables)
  - E.g., hasChild
- ❖ Individuals (constants)
  - E.g., John, Mary



# Description Logics (Syntax)

## □ Description languages

- ❖ Defining complex concepts: sets of individuals
- ❖ Defining complex roles: binary relations on individuals

## □ Complex concepts are built by

- ❖ Atomic concepts: Tissue, Heart
- ❖ Constructors:  $\text{Tissue} \sqcap \exists \text{part-of.Heart}$

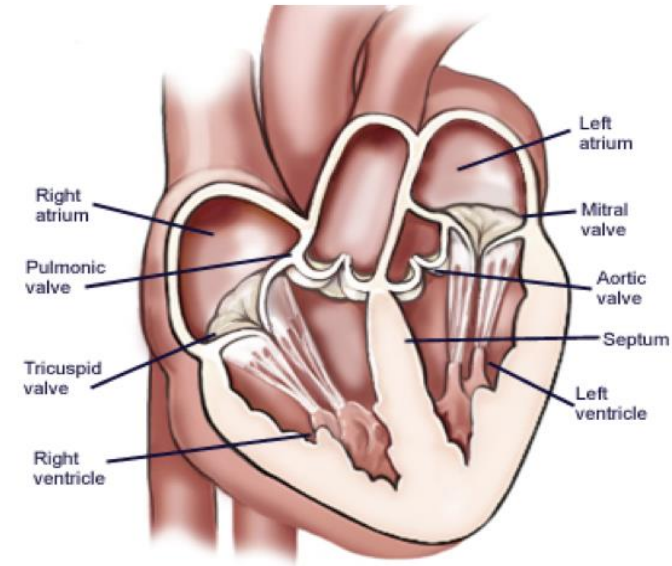
## □ Complex roles are built by

- ❖ Atomic roles: part-of, has-location
- ❖ Constructors: HasFather<sup>-</sup>



# Example

Heart is a muscular organ that  
is part of the circulatory system



Heart  $\sqsubseteq$  Muscular Organ  $\sqcap$   $\sqsupseteq$  part-of. Circulatory System



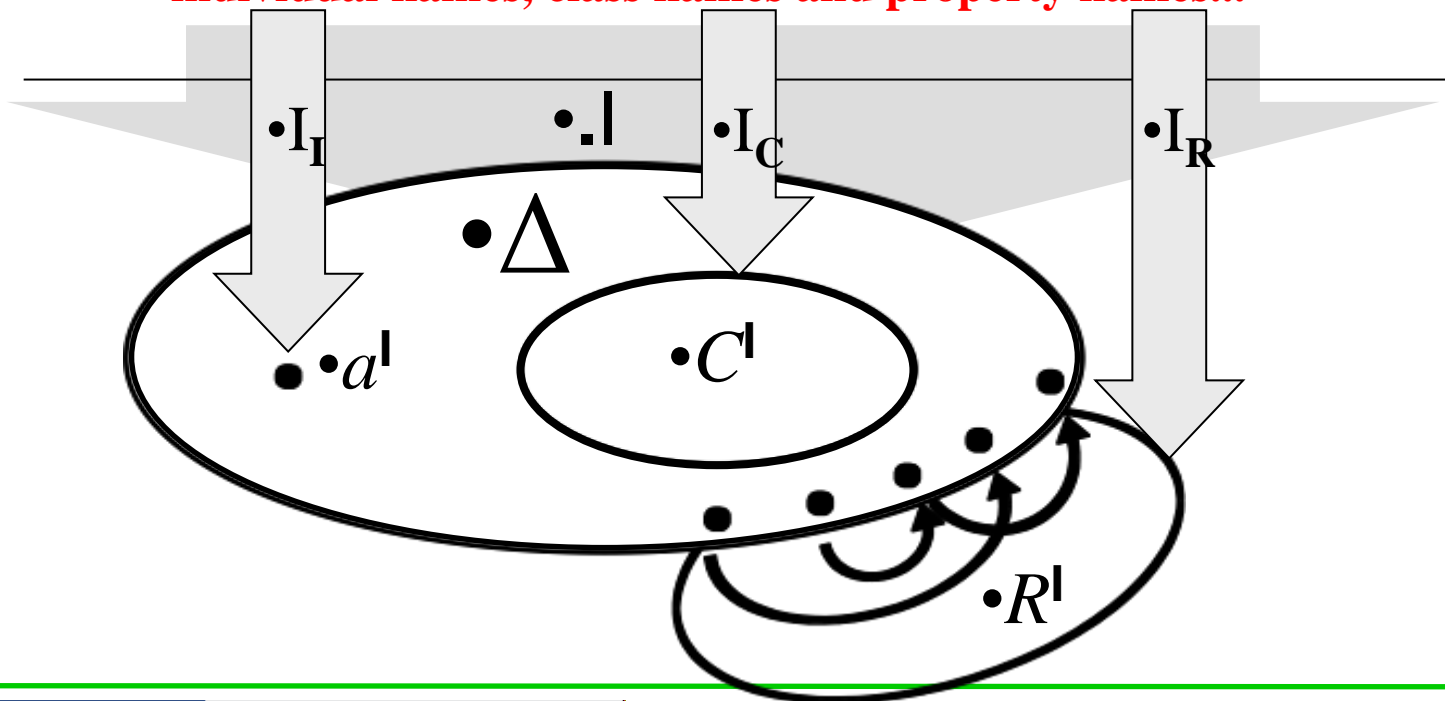
# Description Logics (Semantics)

□ Interpretation:  $\mathbf{I} = (\Delta^{\mathbf{I}}, \cdot^{\mathbf{I}})$

❖ Domain:  $\Delta^{\mathbf{I}}$

❖ Assignment function  $\cdot^{\mathbf{I}}$

individual names, class names and property names...



# Description Logics (Cont.)

□ Interpretation:  $I = (\Delta^I, \cdot^I)$

Construct	Syntax	Example	Semantics
Atomic concept	<b>A</b>	<b>Heart</b>	$A^I \subseteq \Delta^I$
Atomic role	<b>R</b>	<b>part-of</b>	$R^I \subseteq \Delta^I \times \Delta^I$
Negation	$\neg C$	$\neg$ Heart	$\Delta^I \setminus C^I$
Conjunction	$C \sqcap D$	Lawyer $\sqcap$ Doctor	$C^I \cap D^I$
Value restriction	$\forall R.C$	$\forall$ part-of.Wood	$\{a \mid \forall b. (a,b) \in R^I, b \in C^I\}$
...	...	...	...



# Description Logics (Ontology)

## □ TBox T: defining terminology of application domain

### ❖ Inclusion assertion on concept : $C \sqsubseteq D$

Pericardium  $\sqsubseteq$  Tissue  $\sqcap \exists$  part-of.Heart

### ❖ Inclusion assertion on roles: $R \sqsubseteq S$

Part-of  $\sqsubseteq$  has-location

## □ ABox A: stating facts about a specific “world”

### ❖ membership assertion: $C(a)$ or $R(a,b)$

HappyMan(Bob), HasChild(Bob, Mary)



# Description Logics(Semantics)

□ Given an interpretation  $I$

□ Semantics of TBox axioms

$$\diamond I \models C \sqsubseteq D \text{ if } C^I \subseteq D^I$$

$$\diamond I \models R \sqsubseteq S \text{ if } R^I \subseteq S^I$$

□ Semantics of ABox assertions

$$\diamond I \models C(a) \text{ if } a^I \in C^I$$

$$\diamond I \models R(a,b) \text{ if } (a^I, b^I) \in R^I$$



# Description Logics(Semantics)

□ **Model of an ontology**  $O = \langle T, A \rangle$

❖ **I is a model of O if it satisfies all axioms in T and all assertions in A**

□ **Concept satisfiability**

❖ **Concept C is satisfiable in O if  $C^I$  is nonempty for some model I of O**

□ **Ontology Entailment:**

❖  **$O \models \phi$  iff  $I \models \phi$  for all models I of O**



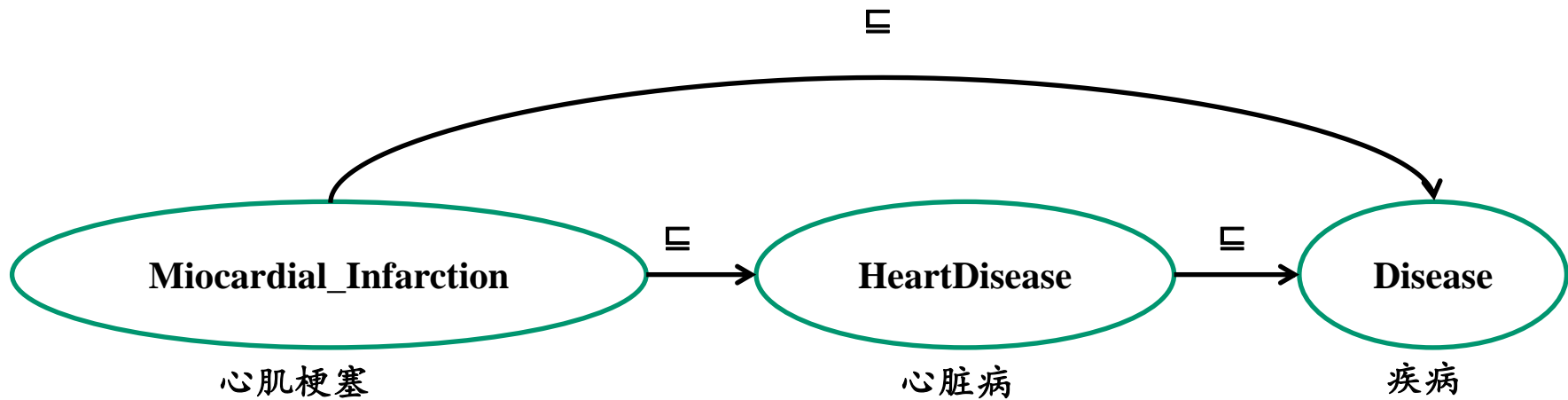


# Conclusion

- ❑ **RDF is a flexible data model for Semantic Web**
- ❑ **RDF Schema provides simple inference capability**
- ❑ **OWL allows more expressive representation of knowledge but is hard to scale to Web data**
- ❑ **Semantic technologies have been adopted by major companies such as Google, Yahoo and Facebook**



# Reasoning Task: Classification



# Reasoning Task: Classification

## Example

**Endocardium**  $\sqsubseteq$  **Tissue**  $\sqcap$   $\exists$  **cont-in.HeartWall**  $\sqcap$   
 $\exists$  **cont-in.HeartValve**

**HeartWall**  $\sqsubseteq$  **BodyWall**  $\sqcap$   $\exists$  **part-of.Heart**

**HeartValve**  $\sqsubseteq$  **BodyValve**  $\sqcap$   $\exists$  **part-of.Heart**

**Endocarditis**  $\sqsubseteq$  **Inflammation**  $\sqcap$   
 $\exists$  **has-loc.Endocardium**

**Inflammation**  $\sqsubseteq$  **Disease**  $\sqcap$   $\exists$  **act-on.Tissue**

**HeartDisease**  $\sqcap$   $\exists$  **has-loc.HeartValve**  $\sqsubseteq$  **CriticalDisease**

**HeartDisease**  $\sqsubseteq$  **Disease**  $\sqcap$   $\exists$  **has-loc.Heart**

**Endocarditis**  $\sqsubseteq$  **HeartDisease**

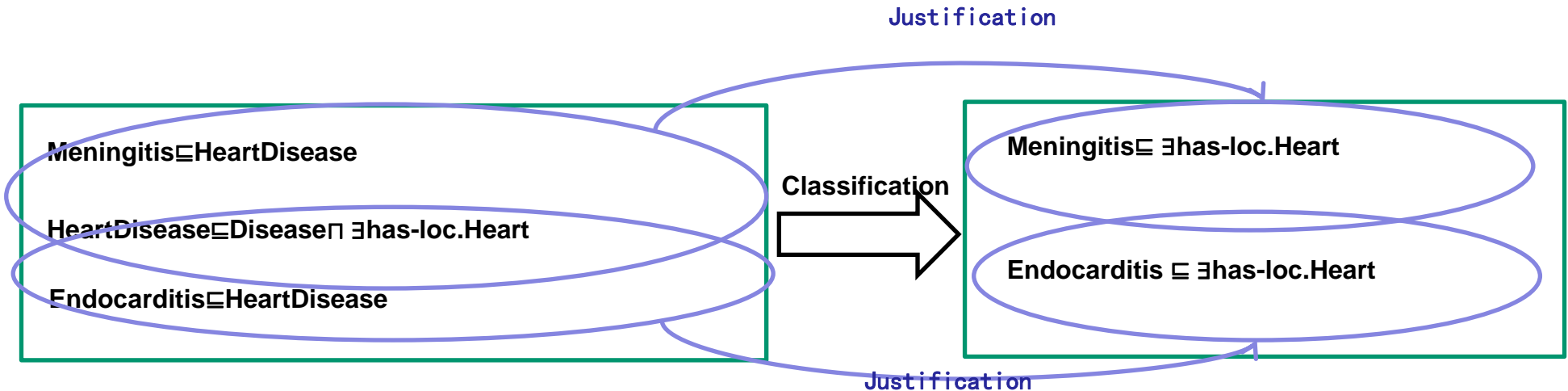
**Endocarditis**  $\sqsubseteq$  **CriticalDisease**

## Role of Classification

- a) Enrich ontology
- b) Query writing
- c) Check satisfiability of KB



# Reasoning Task: Finding Justification



## ❑ Repair KB using justifications

- ❖ Through classification, we have “Meningitis  $\subseteq$   $\exists$ has-loc.Heart”
- ❖ After finding justification, we found “Meningitis  $\subseteq$  HeartDisease” is wrong



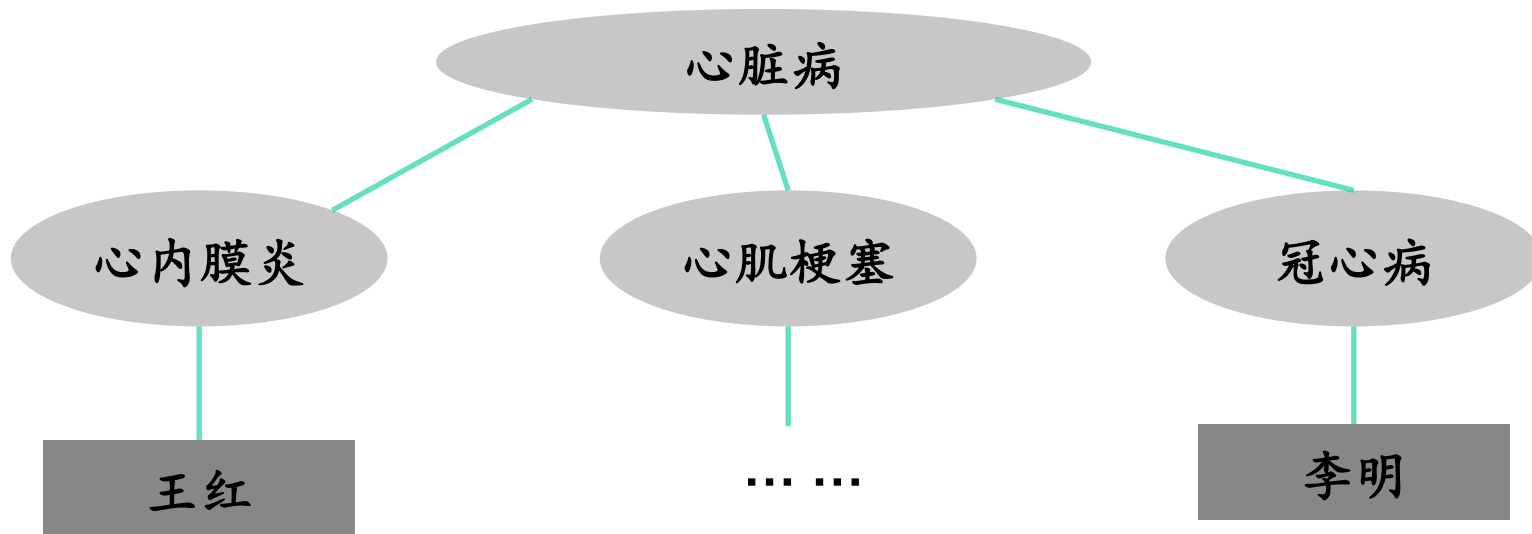
# Reasoning Task: Query Rewriting

- Suppose we have the following query  
“心脏病患者有哪些？”
- This query can be used for medical statistics



# Reasoning Task: Query Rewriting

- Suppose we have the following ontology

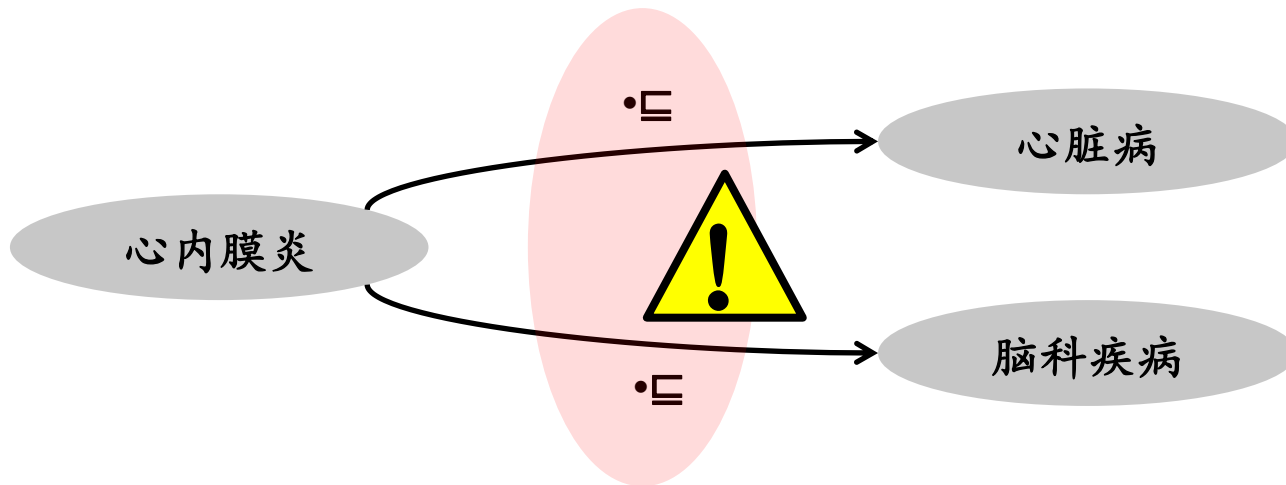


- We know “王红” is 心内膜炎患者, we should include her as心脏病患者

List(X) :- Endocarditis(X)  $\vee$  **Miocardial\_Infarction(X)**  $\vee$  **Coronary\_disease(X)**.

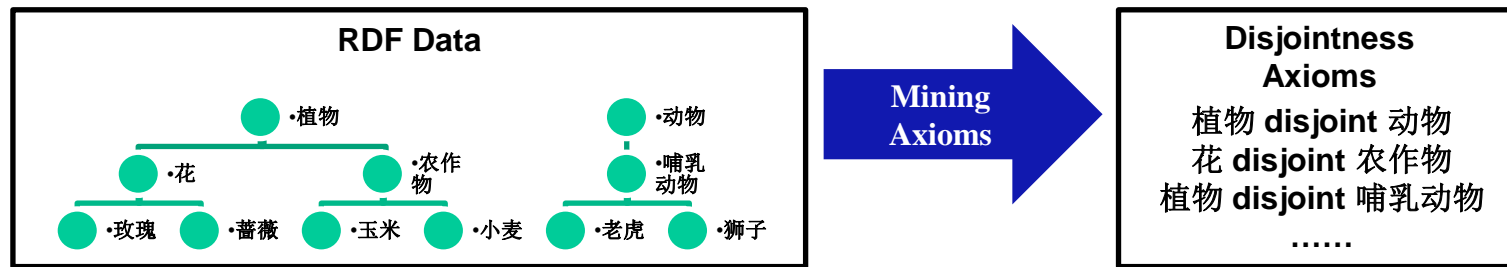
# Reasoning Task: Checking Inconsistency

- ❑ Inconsistency may occur during ontology construction
  - ❖ One source of inconsistency comes from disjoint axioms



# Reasoning Task: Checking Inconsistency

- Mining disjoint Concepts: Association rule mining, Inductive logic programming



- In Zhishi.me, hudong:大豆食心虫 not only belongs to animal but also contains in plant
- In Zhishi.me, there are 50 common instances between animal and plant



# Reasoning Task: Checking Inconsistency

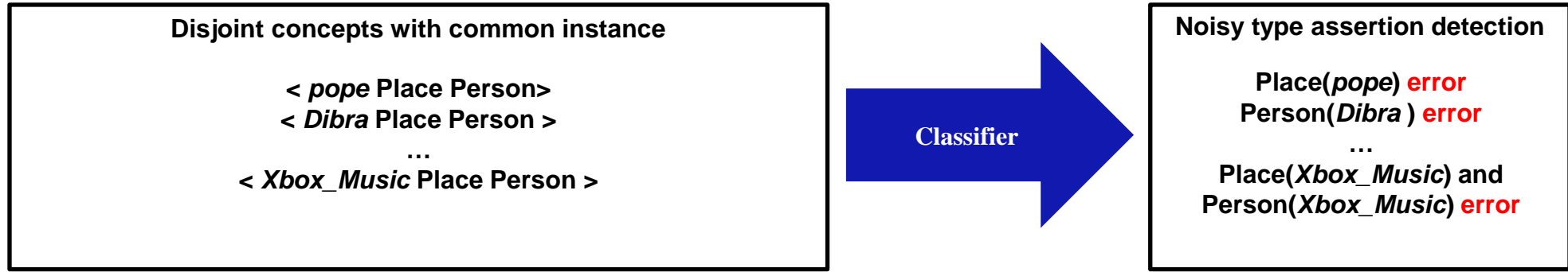
- In Dbpedia, we find 42153 disjointness axioms by mining axioms algorithm

Number of Common individuals	Pairs of disjoint classes
[1,10)	317
[10,100]	27
[100,1000)	7



# Reasoning Task: Checking Inconsistency

## □ Detecting noisy type assertion



## □ Experiment result of detecting noisy type assertion in DBpedia

Classifier	Precision	Recall	F1-Measure
J48	93.6%	93.6%	93.6%
J48(boost)	95.6%	95.6%	95.6%

# Reasoning with Large Scale Imprecise Knowledge on the Semantic Web



# Motivation

- ❑ More and more semantic data are published and linked
- ❑ Semantic data are inherently imprecise
  - ❖ Data extraction may result in imprecision
  - ❖ Data linking may result in imprecision
  - ❖ Reasoning with large imprecise semantic data
- ❑ Schema of the data may also be imprecise
  - ❖ Schema induction
  - ❖ Ontology enrichment
  - ❖ Reasoning with large imprecise ontologies

# Background: Fuzzy pD\*

## Fuzzy Logic

A fuzzy statement is in form of  $\phi[n]$

$\phi$  is a statement

$n$  is called the fuzzy degree ( $n \in [0,1]$ )

T-norm operator

Lukasiewicz Logic

$$a \otimes b = \max(a + b - 1, 0)$$

Godel Logic

$$a \otimes b = \min(a, b)$$

Product Logic

$$a \otimes b = a \cdot b$$

## Fuzzy RDF triple

(Tom, like, pizza)[0.8]



# Background: Fuzzy $pD^*$

## Fuzzy $D^*$ rule

E.g. rule f-rdfs2 :

$$(p, \text{domain}, u)[n], (v, p, w)[m] \Rightarrow (v, \text{type}, u)[n \otimes m]$$

## Fuzzy $P$ rules

E.g. rule f-rdfsp4

$$(p, \text{type}, \text{TransitiveProperty})[n], (a, p, b)[m], (b, p, c)[k] \\ \Rightarrow (a, p, c)[n \otimes m \otimes k]$$

## Best Degree Bound

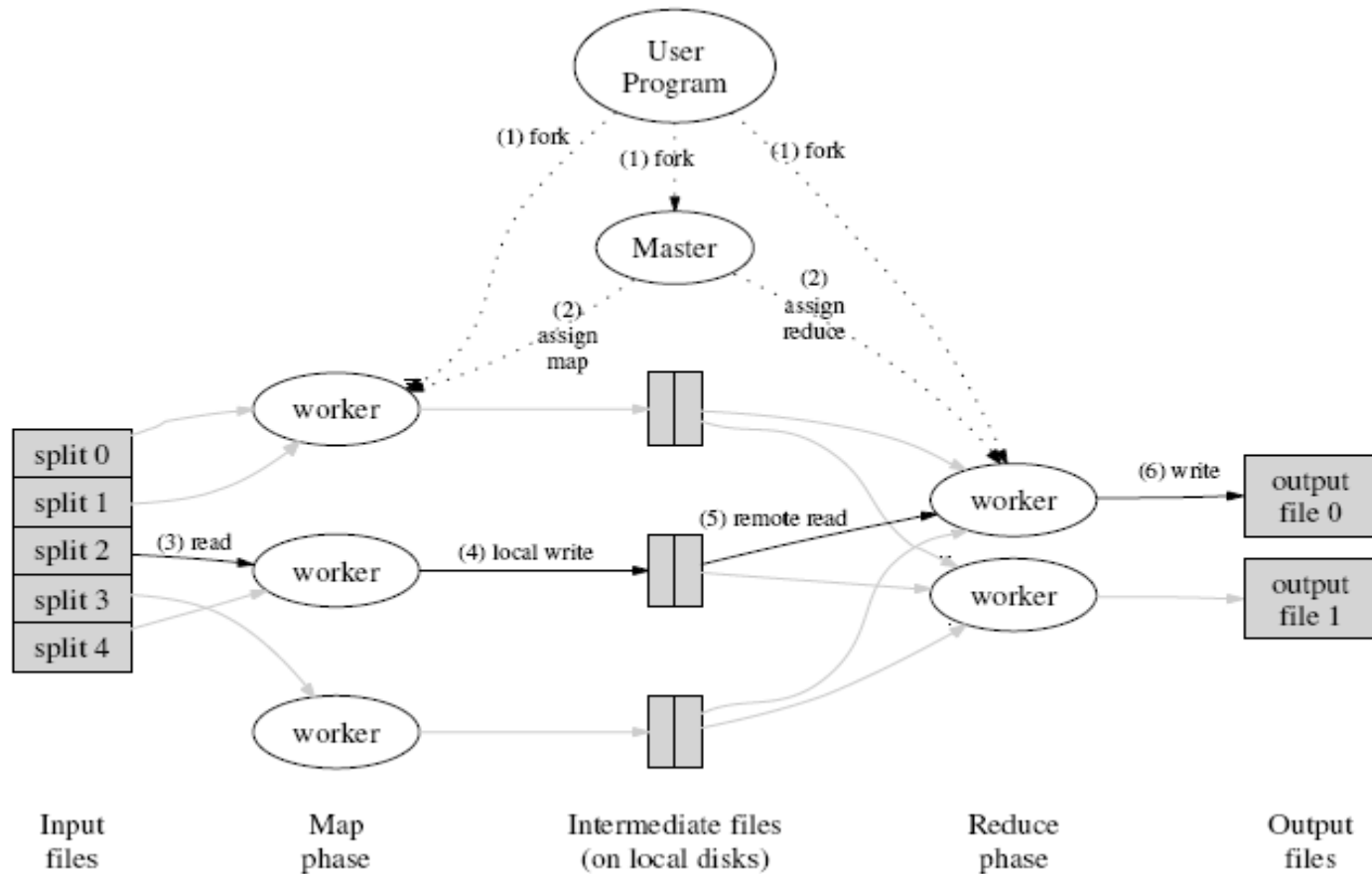
$$(a, \text{type}, u)[0.5], (a, p, b)[0.9], (p, \text{domain}, u)[1]$$

$$\text{Since } (a, p, b)[0.9], (p, \text{domain}, u)[1] \Rightarrow (a, \text{type}, u)[0.9]$$

The BDB of  $(a, \text{type}, u)$  is 0.9

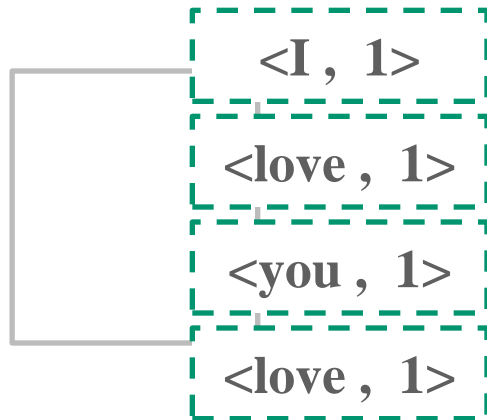


# MapReduce

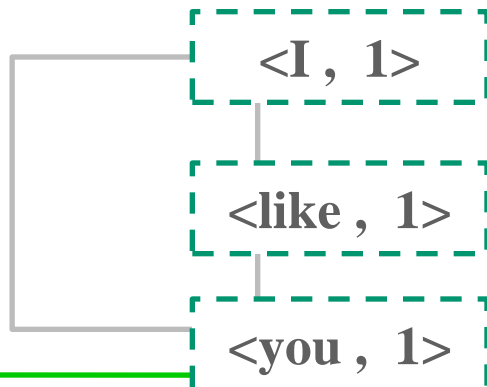


# Example

I love  
you  
love



I like  
you



Reducer  
1  
(I)

<I, 2>

Reducer  
2  
(love)

<love, 2>

Reducer  
3  
(you)

<you, 2>

Reducer  
4  
(like)

<like, 1>



# Challenges

## Ordering the rule applications

Bad orders will generate more non-BDB fuzzy triples

## The shortest path calculation

Some rules essentially calculates the all-pair shortest paths

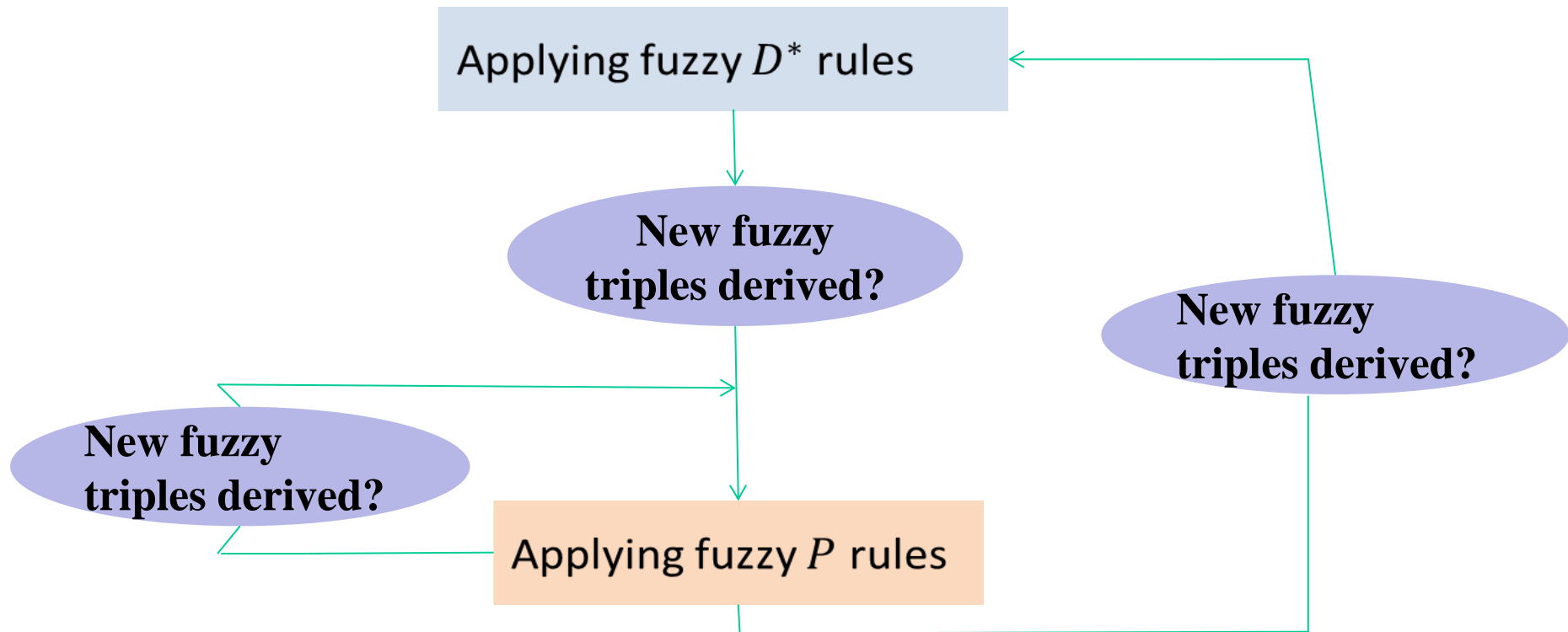
## Sameas rules

Canonical representation technique is not applicable to handle the semantics of vague sameas triples



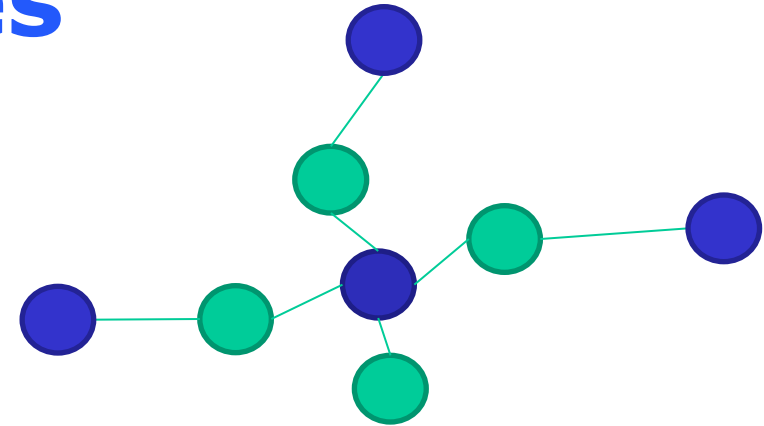
# Ordering the rule applications

## □ Control flow of the reasoning algorithms





# Sameas rules



Traditional Method

Canonical representation

Drawback

**Vague sameas triples**

$(a, \text{sameas}, b)[0.8] (b, \text{sameas}, c)[0.1] (c, \text{sameas}, d)[0.8]$

$(a, \text{range}, r)[0.9] (u, b, v)[0.9] (c, \text{domain}, e)[1] (u', d, v')[0.9]$

There is no canonical representation!

If we choose  $c$  as the representation

the RDF graph will be converted into

$(c, \text{range}, r)[0.1] (u, c, v)[0.1] (c, \text{domain}, e)[1] (u', c, v')[0.8]$

The BDB of  $(v, \text{type}, r)$  is 0.1

However the BDB of  $(v, \text{type}, r)$  in the original graph is 0.8

# Setting

## □ Dataset

- ❖ Weighted DBPedia core ontology
- ❖ wpdLUBM 1000, 2000, 4000, 8000

## □ Cluster

- ❖ 25 machine with at most 75 mapper/reducer slots



# Experiment

□ Dataset: Weighted DBPedia core ontology

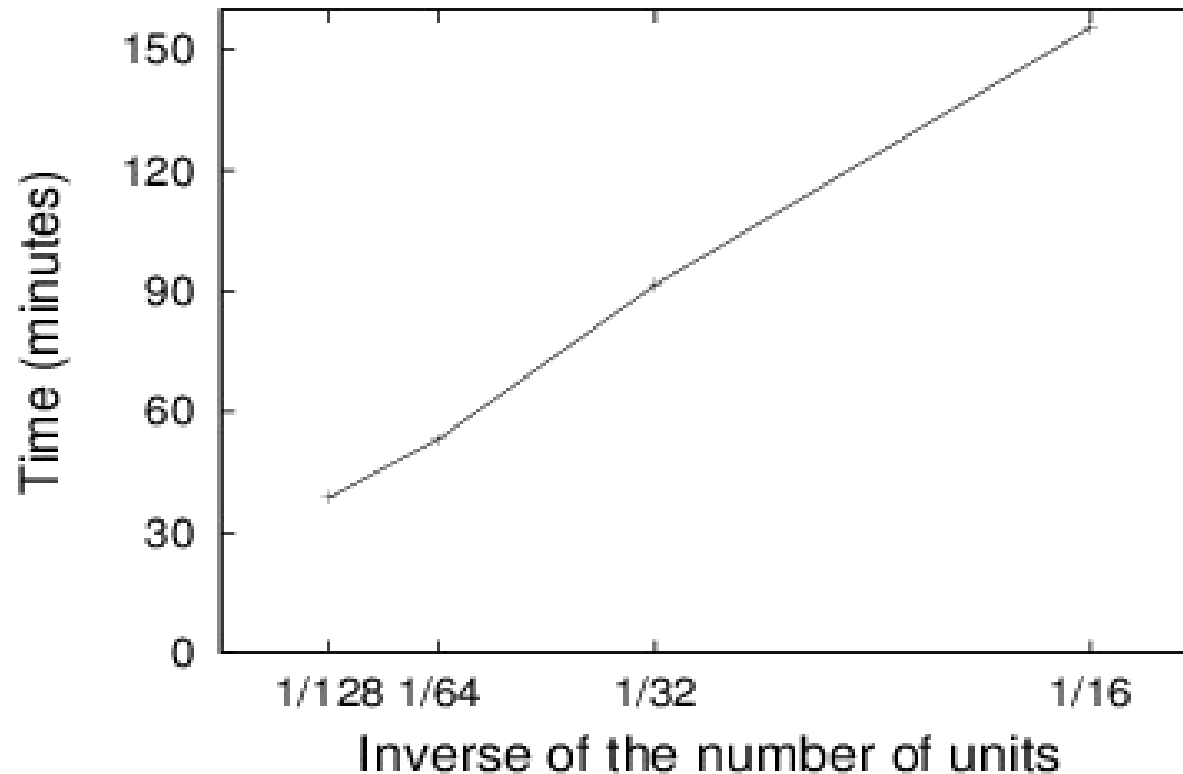
□ Results:

#units	128	64	32	16	8	4	2
Time(sec.)	122.653	136.861	146.393	170.859	282.802	446.917	822.269
Speedup	6.70	6.01	5.62	4.81	2.91	1.84	1.00



# Experiment

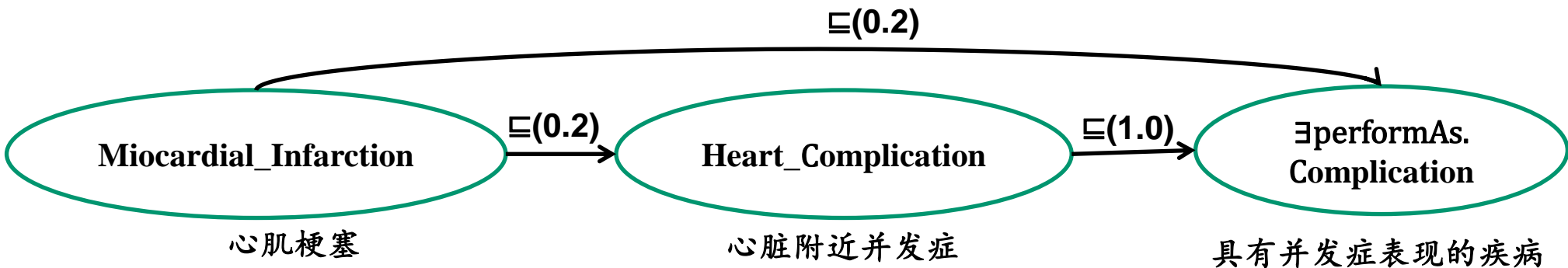
## □ Scalability over number of units



# Reasoning on fuzzy-EL+

## □ Classification rules for fuzzy-EL+

**R2** If  $\langle A, n \rangle \in S(X)$ ,  $\langle A \sqsubseteq \exists r.B, k \rangle \in O$ , and  $\langle X, B, m \rangle \notin R(r)$ , where  $m = \min(n, k)$   
then  $R(r) := R(r) \cup \{\langle X, B, m \rangle\}$ , where  $m = \min(n, k)$





# Challenges and methods

- ❑ Transforming rule-applying to an operation on tables
- ❑ The rules are given by operations on sets. It is more straightforward to treat them as operations on tables, in other words, relation algebra

R2:

$$\langle A, n \rangle \in S(X), \quad \langle A \sqsubseteq \exists r.B, k \rangle \in O \quad \Rightarrow \quad \langle X, B, m \rangle \in R(r)$$

R2:

$$(X, A, n) \in S, \quad (A, r, B, k) \in O_{\sqsubseteq \exists} \quad \Rightarrow \quad (r, X, B, m) \in R$$

$$(S \bowtie_A O_{\sqsubseteq \exists}) \cup R$$



# Challenges and methods

❑ Handling multi-way join

❑ MapReduce can handle a 2-way join in one job.

R2 (  $(S \bowtie_A O_{\exists \exists}) \cup R$  ) and R4, contain one 2-way join. They can be easily handled by MapReduce.

R1 contains a complex multi-way join.

$$\mathbf{R1: (S \bowtie_X \dots \bowtie_X S \bowtie_{A_1 \dots A_l} O_{\cap \exists}) \cup S}$$

R3 and R5 contains a 3-way join.

$$\mathbf{R3: (R \bowtie_Y S \bowtie_A O_{\exists \exists}) \cup S}$$

$$\mathbf{R5: (R \bowtie_Y R \bowtie_{r,s} O_{\circ \exists}) \cup R}$$

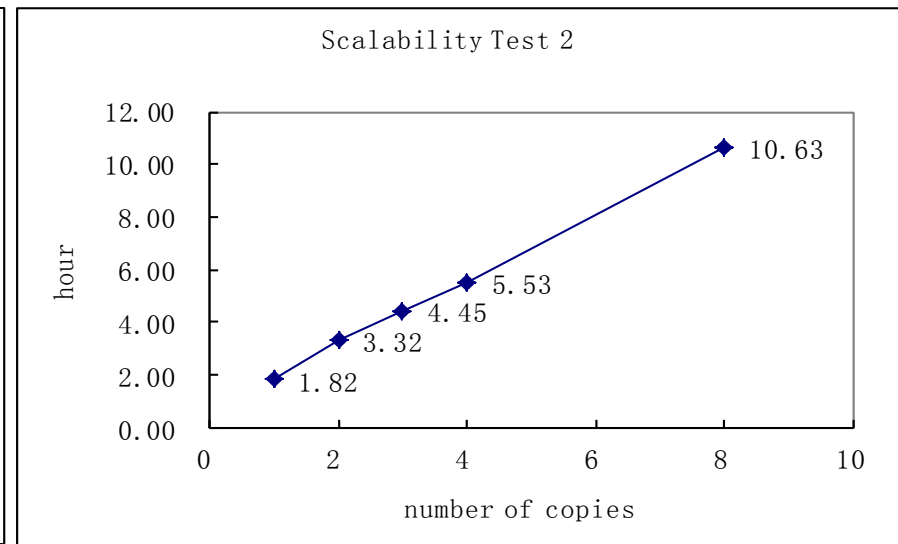
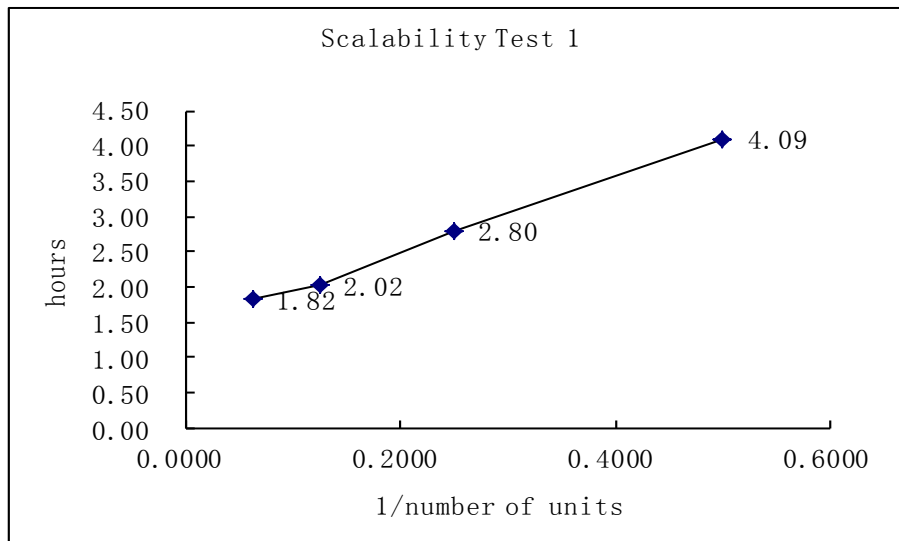
Basic idea: Transforming a 3-way join to two 2-way joins.



# Evaluation on Galen

- EL-Galen
- 8nodes, 16 units

Concepts	Roles	GCI	RI
47,840	1,892	87,594	1,947



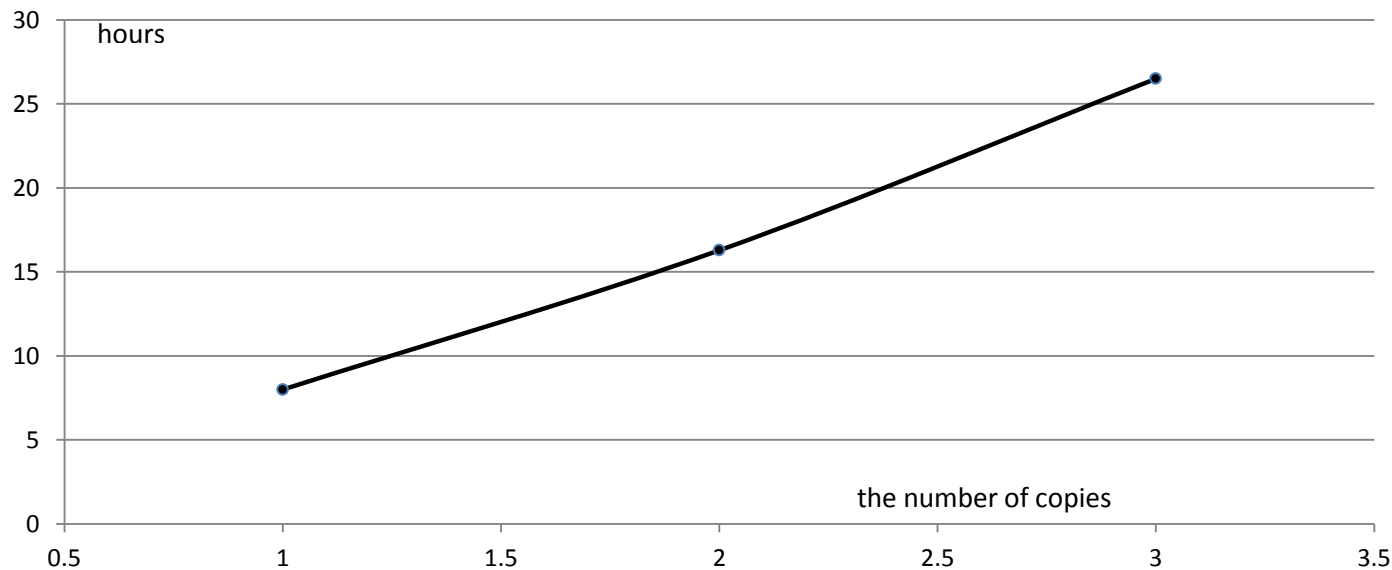
- Scalability test 1: The system's performance speeds up linearly to the increase of number of units
- Scalability test 2: The cost time increases linearly to the number of copies of the input ontology



# Evaluation on Snomed-CT

## •Snomed-CT

Concepts	Roles	GCI	RI
836,612	77	1,438,948	23



•Scalability test: The cost time increases linearly to the number of copies of the Snomed-CT



# Conclusion and Discussion

- ❑ **Ontology reasoning plays an important role for KG**
  - ❖ Detecting logical inconsistency and repair knowledge bases (improve the quality of the knowledge)
  - ❖ Extend knowledge bases (materialization, classification)
  - ❖ Query rewriting and extension
- ❑ **Reasoning in KG need meta-reasoning**
  - ❖ Variety of knowledge: terminological knowledge, rule, probabilistic knowledge ect.
- ❑ **Challenging problems**
  - ❖ Current work is mainly based on MapReduce and Hadoop, thus suffers from the problem of efficiency and dynamics
  - ❖ Only lightweight ontology languages, such as RDFS, OWL 2 RL are supported
  - ❖ Reasoning with imprecise knowledge is not well discussed

